

DTU



Marvin Beckmann, Christian Majenz

Fully Anonymous Ring Signatures in the QRROM

Example: Whistleblowers



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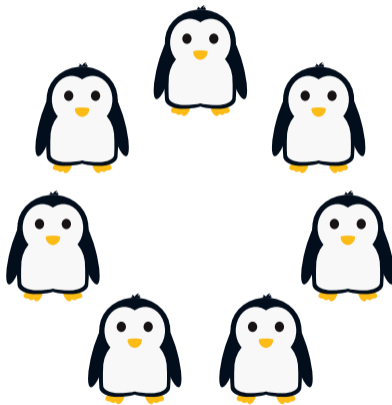


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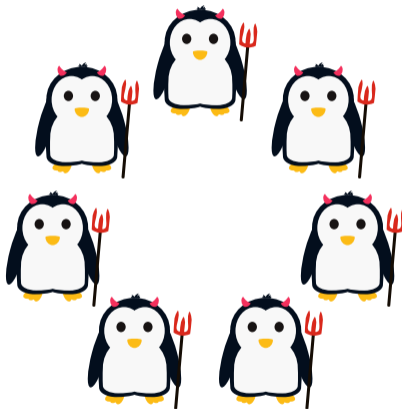


Deniability and Authenticity

Ring Signatures



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(1) AOS-transform [1] and (2) Ring Trapdoor Functions

Sigma Protocols

Prover(inst, w)

$(\text{com}, \text{state}) \leftarrow P_1(\text{inst})$

com



ch



$\text{rsp} \leftarrow P_2(\text{state}, w, \text{ch})$

rsp

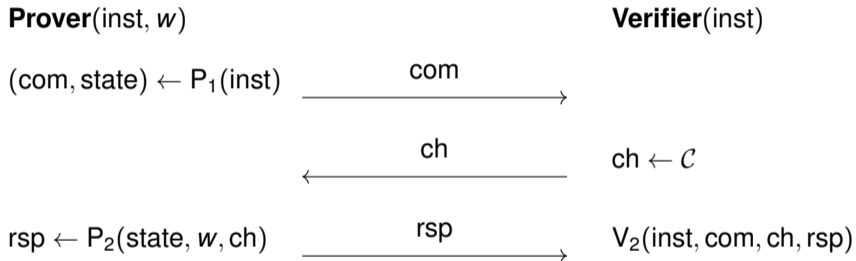


Verifier(inst)

$\text{ch} \leftarrow \mathcal{C}$

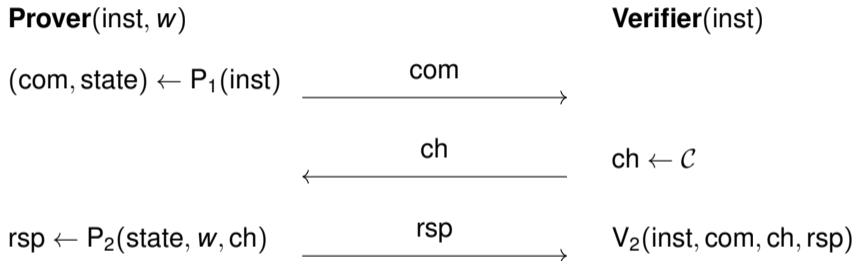
$V_2(\text{inst}, \text{com}, \text{ch}, \text{rsp})$

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- Impersonation, . . . , witness recovery, HVZK simulator (with min-entropy)

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- To make a signature scheme: Fiat-Shamir transform

AOS Transform for Sigma Protocols

$\text{Sign}(\text{sk}_j = w_i, \rho = \{\text{inst}_1, \dots, \text{inst}_N\}, \mu)$

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2 :

3 :

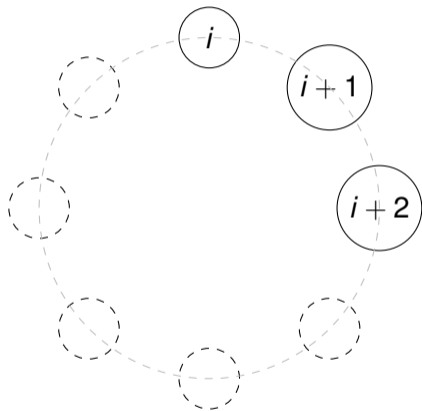
4 :

5 :

6 :

7 :

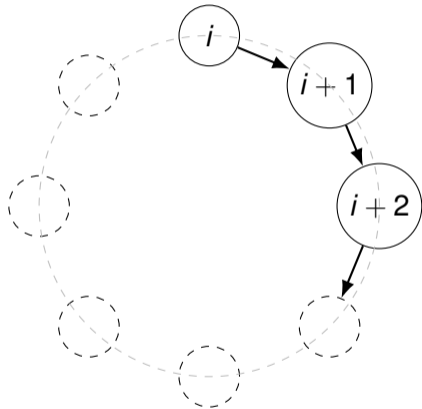
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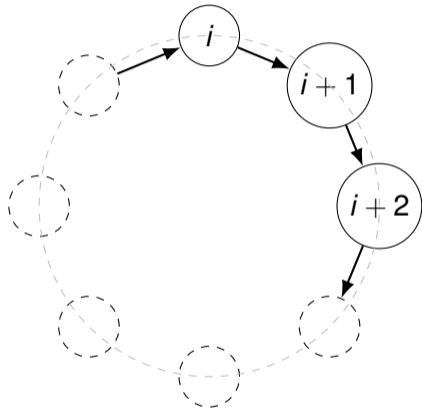
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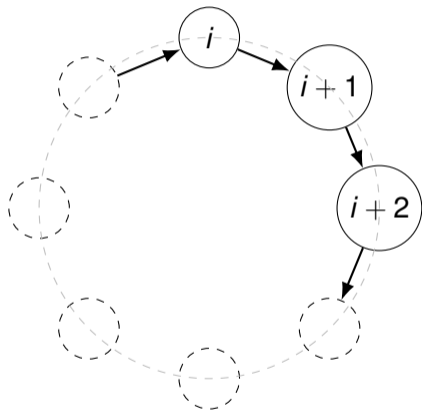
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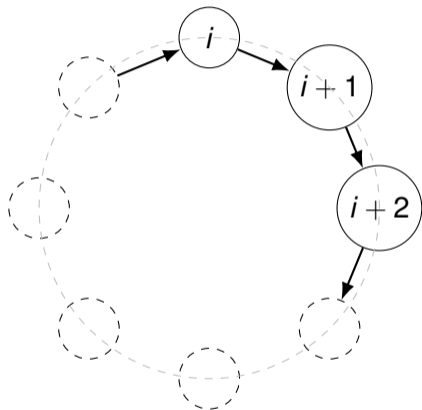
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- 7: $\sigma \leftarrow ((\text{com}_1, \text{rsp}_1), \dots, (\text{com}_N, \text{rsp}_N))$
- 8: **return** σ



A QROM-Proof for AOS

Goal: Reduce ring signature unforgeability to impersonation security

¹ multiplicative loss exponential in ring size

² Additive error term

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 - general approach: using measure-and-reprogram [4], get an order of all queries from a forgery¹
 - alternative approach: assume commit-and-open sigma protocols: use framework [3] based on Zhandry's compressed oracle slightly adjusted in [5]²

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Commit-and-Open Protocols for AOS

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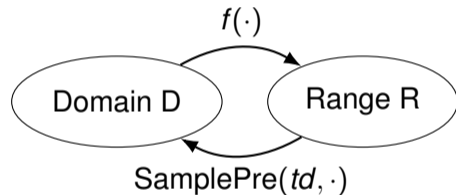
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 - depends on maximal fraction of challenges that can be answered for a fixed commitment without extraction being possible

Yay, QROM Proofs for AOS Ring Signatures!



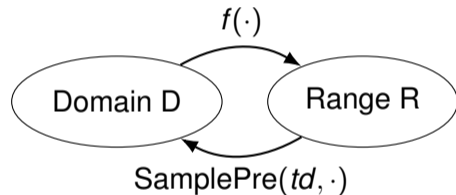
Trapdoor Functions and PSFs [6]

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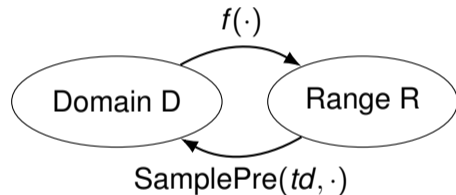
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- We again define PSF-like properties³

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Ring Trapdoor Functions for Ring Signatures

Sign(sk, ρ , m)

1 : $\mathbf{s} \leftarrow \{0, 1\}^\lambda$

2 : $h \leftarrow H(\rho, \mathbf{s}, m)$

3 : $\sigma \leftarrow \text{SamplePre}(\text{sk}, \rho, h)$

4 : **return** (\mathbf{s}, σ)

^arequires statistical distance ϵ and yields additive term of $\approx q^2 \sqrt{\epsilon}$

Ring Trapdoor Functions for Ring Signatures

1 query simulation strategy

- sample in domain D_ρ and apply f_ρ
- do a history-free proof [2]; use randomness (deterministically derived from ρ, s, m) for domain sampling^a

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Summary

QROM proof for

- AOS-transform
 - General bound with multiplicative term of q^{2N}
 - Commit-and-open additive term
- Preimage sampleable ring trapdoor function
 - only work with statistical distance ^a

^aWe are working on changing this



References I

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